

What is claimed is:

1. A method for projecting a superimposed image onto a target display surface under observation of at least one camera, the method comprising the steps of:

5 (a) determining a projective relationship between each of a plurality of projectors and the target display surface;

(b) estimating a component image for each said projector, comprising:

10 (1) using said projective relationship, for each of said component images determine a plurality of sub-sampled, regionally shifted images represented in the frequency domain; and

(2) composing each said component image using a respective plurality of said sub-sampled, regionally shifted images; and

15 (c) minimizing the difference between a sum of said component images and a frequency domain representation of a target image to produce a second component image for each said projector.

2. The method of claim 1 wherein said step of minimizing the difference between said sum and said frequency domain representation of said target image comprises: (a) identifying a second set of frequency domain coefficients for use in producing a frequency domain representation of said second component image for a respective one of said projectors, and (b) taking the inverse Fourier transform of said frequency domain representation of said second component image for said respective one of said projectors; and further comprising the step of projecting from each said projector, a respective one of said second component images to produce the superimposed image.

25 3. The method of claim 1 wherein said step of determining a projective relationship further comprises:

(a) observing the target display surface with the camera, c ;

(b) recovering a homography between each projector, p_i , and the camera,

30 $H_{p_i}^c$, and

(c) using said homography, $H_{p_i}^c$, determine said projective relationship, $H_{p_i}^b$,

wherein b represents a reference frame for the target display surface.

4. The method of claim 2 wherein said step of using said projective relationship to determine said plurality of sub-sampled, regionally shifted images, comprises: (a) decomposing each said projective relationship, $H_{p_i}^b$, into a linear shift matrix representing offsets between a respective of said projectors p_i , and said reference frame b; and (b) using said linear shift matrix for said determining said plurality of sub-sampled, regionally shifted images associated with said respective of said projectors p_i .

5 5. The method of claim 1 wherein said step of minimizing the difference between said sum and said frequency domain representation of said target image, $F_r[u, v]$, comprises:

10 (a) minimizing the expression:

$$\left\| F_r[u, v] - \left(\sum_{i=0}^k F_{\Delta}^i[u, v] \right) \right\|^2$$

15 wherein k represents the total number of said plurality of projectors, said component image for each said projector is represented by $F_{\Delta}^p[u, v] = \sum_{r=0}^N F_{\Delta_r}[u, v]$, and said sub-sampled, regionally shifted images represented in the frequency domain are represented by $F_{\Delta_r}[u, v]$, to identify a second set of frequency domain coefficients for use in producing a frequency domain representation of said second component image for a respective one of said projectors; and

20 (b) taking the inverse Fourier transform of said frequency domain representation of said second component image for said respective one of said projectors.

25 6. A system for projecting the superimposed image onto the target display surface, of claim 1, wherein: being projected from each said projector, is a respective one of said second component images to produce the superimposed image.

7. A method for projecting a superimposed image onto a target display surface under observation of at least one camera, the method comprising the steps of:

30 (a) determining a projective relationship between each of a plurality of projectors and the target display surface;
(b) estimating a component image for each said projector, comprising:

(1) using said projective relationship, for each of said component images determine a plurality of sub-sampled, regionally shifted images represented in the frequency domain, and

(2) composing each said component image using a respective plurality of said sub-sampled, regionally shifted images; and

5 (c) performing an optimization using said component images and a frequency domain representation of a target image to produce a second component image for each said projector.

10 8. The method of claim 7 wherein:

(a) said step of performing an optimization comprises minimizing the difference between a sum of said component images and said frequency domain representation of said target image, $F_r[u, v]$, to produce said second component image for each said projector; and

15 (b) said step of determining a projective relationship further comprises:

(1) observing the target display surface with the camera, c ;

(2) recovering a homography between each projector, p_i , and the camera, $H_{p_i}^c$; and

(3) using said homography, $H_{p_i}^c$, determine said projective relationship, $H_{p_i}^b$, wherein b represents a reference frame for the target display surface.

20

9. The method of claim 8 wherein said step of performing an optimization comprises minimizing the difference between a sum of said component images and said frequency domain representation of said target image, $F_r[u, v]$, by minimizing the expression:

25

$$\left\| F_r[u, v] - \left(\sum_{i=0}^k F_{\Delta}^i[u, v] \right) \right\|^2$$

wherein k represents the total number of said plurality of projectors, said component image for each said projector is represented by $F_{\Delta}^p[u, v] = \sum_{r=0}^N F_{\Delta r}[u, v]$, and said sub-sampled, regionally shifted images represented in the frequency domain are represented by $F_{\Delta r}[u, v]$,

30

to identify a second set of frequency domain coefficients for use in producing a frequency

domain representation of said second component image for a respective one of said projectors.

10. A system for projecting the superimposed image onto the target display surface, of

5 claim 7, wherein: being projected from each said projector, is a respective one of said second component images to produce the superimposed image.

11. A computer executable program code on a computer readable storage medium for

projecting a superimposed image onto a target display surface under observation of at least

10 one camera, the program code comprising:

(a) a first program sub-code for determining a projective relationship between each of a plurality of projectors and the target display surface;

(b) a second program sub-code for estimating a component image for each said projector, said second program sub-code comprising instructions for:

15 (1) using said projective relationship, for each of said component images determine a plurality of sub-sampled, regionally shifted images represented in the frequency domain; and

(2) composing each said component image using a respective plurality of said sub-sampled, regionally shifted images; and

20 (c) a third program sub-code for minimizing the difference between a sum of said component images and a frequency domain representation of a target image to produce a second component image for each said projector.

25 12. The program code of claim 11 wherein said frequency domain representation of said

target image as $F_r[u, v]$, and said third program sub-code comprises instructions for:

(a) minimizing the expression:

$$\left\| F_r[u, v] - \left(\sum_{i=0}^k F_{\Delta}^i[u, v] \right) \right\|^2$$

wherein k represents the total number of said plurality of projectors, said component

30 image for each said projector is represented by $F_{\Delta}^0[u, v] = \sum_{r=0}^N F_{\Delta r}[u, v]$, and said sub-

sampled, regionally shifted images represented in the frequency domain are represented by $F_{\Delta r}[u, v]$, to identify a second set of frequency domain coefficients for

use in producing a frequency domain representation of said second component image for a respective one of said projectors; and

5 (b) taking the inverse Fourier transform of said frequency domain representation of said second component image for said respective one of said projectors.

13. A computer executable program code on a computer readable storage medium for projecting a superimposed image onto a target display surface under observation of at least one camera, the program code comprising:

10 (a) a first program sub-code for determining a projective relationship between each of a plurality of projectors and the target display surface;

(b) a second program sub-code for estimating a component image for each said projector, said second program sub-code comprising instructions for:

15 (1) using said projective relationship, for each of said component images determine a plurality of sub-sampled, regionally shifted images represented in the frequency domain; and

(2) composing each said component image using a respective plurality of said sub-sampled, regionally shifted images; and

20 (c) a third program sub-code for performing an optimization using said component images and a frequency domain representation of a target image to produce a second component image for each said projector.

14. The program code of claim 13 wherein:

25 (a) said third program sub-code comprises instructions for minimizing the difference between a sum of said component images and said frequency domain representation of said target image to produce said second component image for each said projector; and

30 (b) said first program sub-code comprises instructions for, while observing the target display surface with the camera, c , recovering a homography between each projector, pi , and the camera, H_{pi}^c ; and using said homography, H_{pi}^c , determining said projective relationship, H_{pi}^b , wherein b represents a reference frame for the target display surface.